

Fast pQCD Calculations for QCD Fits

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*fast***NLO**

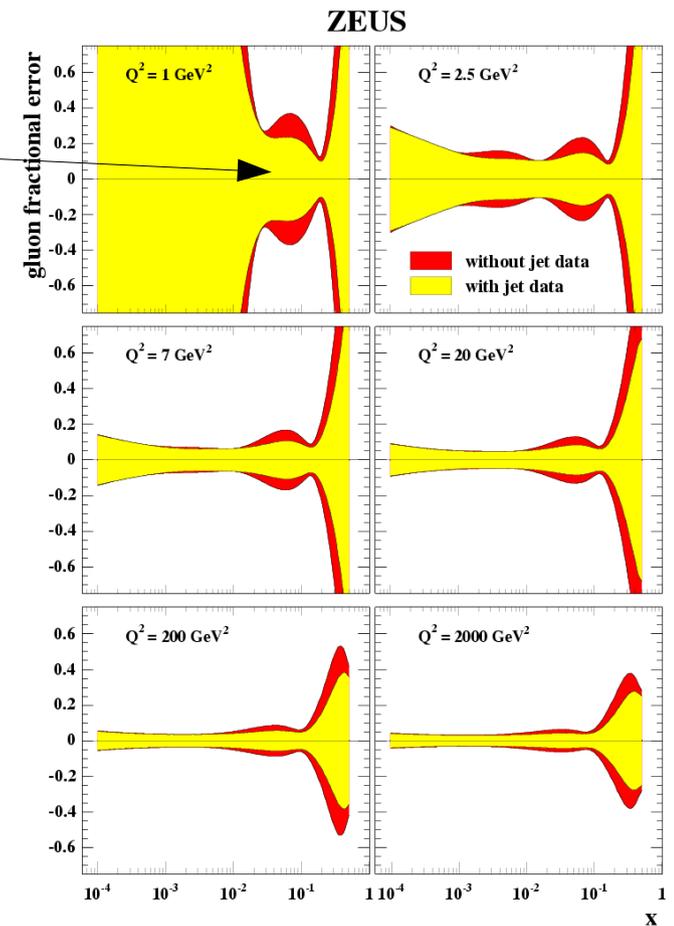
`http://hepforge.cedar.ac.uk/fastnlo`

basic concept: shown e.g. in talks at DIS06, TeV4LHC

this talk: status of project, selected details

Motivation

- Wealth of jet measurements from HERA and TEVATRON not yet exploited by global pdf fits
- Jets give additional constraints on gluon at higher x
- Exclusive variables, need time consuming MC integration
- Required for fits: fast and precise prediction as function of α_s and pdfs
- Key: separate integration of ME from α_s and pdf



CPU weeks, months, years

Calculate once per measured data set
Save in

Table

0.5 ms

Plug in pdf and α_s
Get cross section

Produce **ready to use** packages for pdf fitters

Package contains precalculated table, FORTRAN (alternative: C++) code returns cross sections, with interface to α_s and pdfs

Results in bins and units etc. as published

Provide info of stat. and syst. precision of the result binwise

Up to now: use NLOJET++ for DIS and hadron-hadron at NLO
plus 2-loop threshold corrections (hadron-hadron) Kidonakis, Owens
Tables available for HERA, TEVATRON, RHIC, LHC
Product **available** for download since June, 5, 2006

Not only fits, convenient for estimation of theory uncertainties, etc.
fastNLO going to be used for upcoming publications of H1, ZEUS, D0, STAR

Bonus: quick and easy access to cross sections via web interface

*remaining part of the talk, details about precision, efficiency,
some results, plans*

Efficiency of pdf interpolation

Need to interpolate pdfs between discrete points in x

Hadron-hadron: no brute force (ultra fine binning) due to **quadratic growth** of table

Get best precision for given number of x "bins"

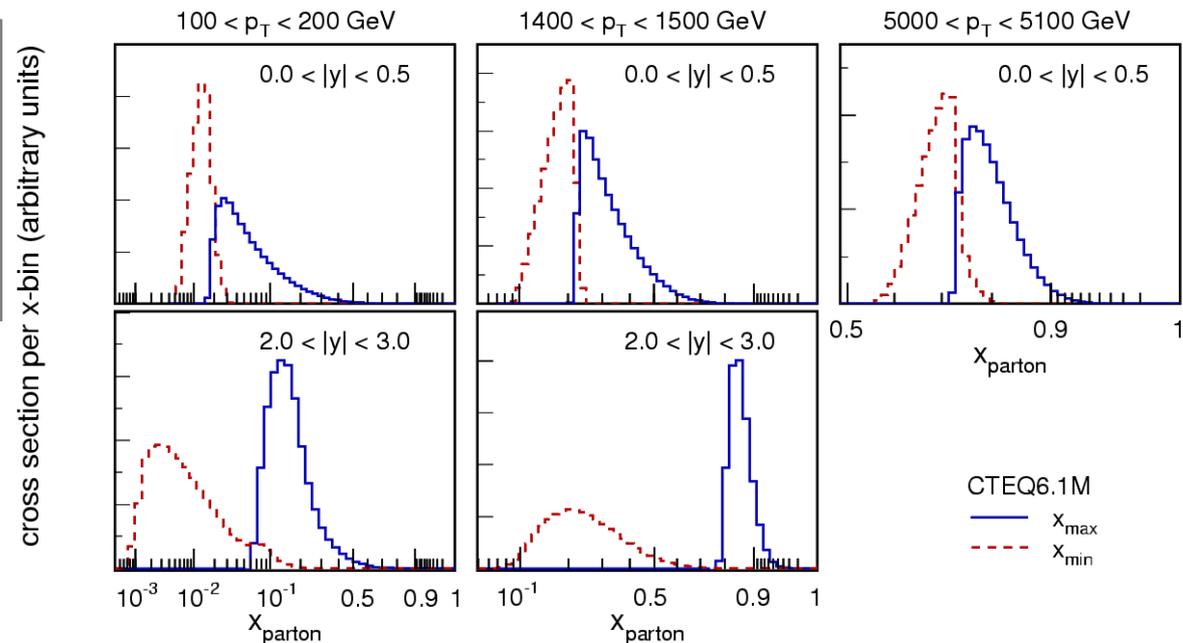
Crucial: steep, curved regions

Need many points there: equidistant bins after transformation, here $\sqrt{\log(1/x)}$

LHC inclusive jet scenario

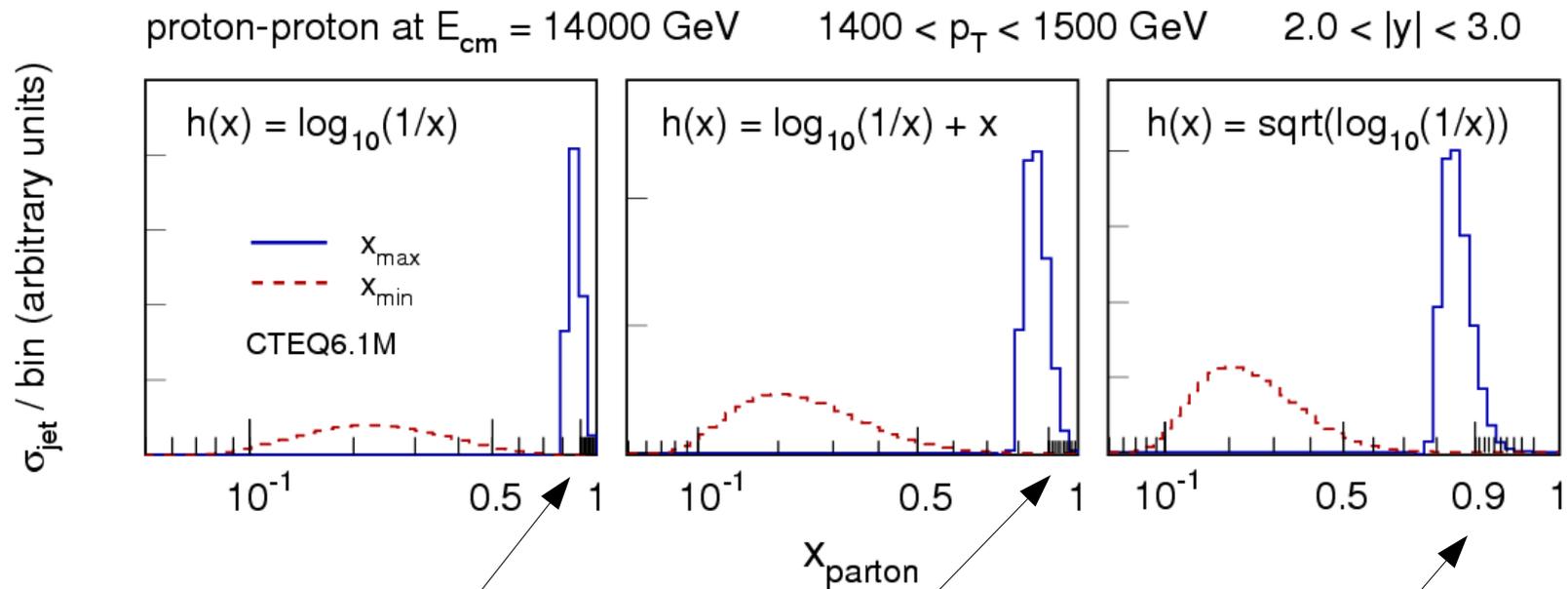
$x_1, x_2 \rightarrow x_{\min}, x_{\max}$ (exploit symmetry)

Issue: **forward region**
phasespace squeezed into small range,
reason for $\sqrt{\log(1/x)}$



Efficiency of pdf interpolation

Advantage of $\sqrt{\log(1/x)}$ to other transformation functions (example):



#bins for $x_{\text{max}} > 0.9$:

3

4

8

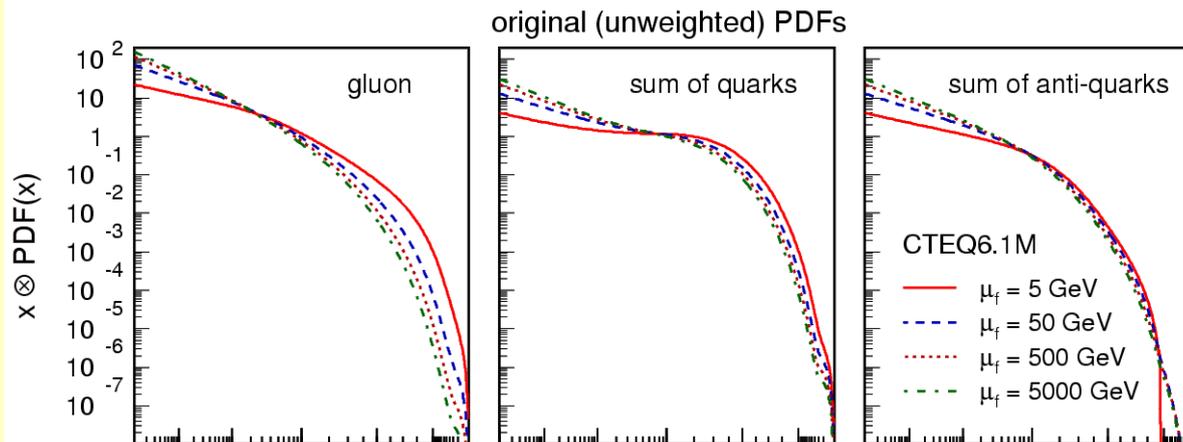
Reweighting

Interpolation of pdfs hampered by curvature

Reweight pdfs! Instead $x \cdot \text{pdf}(x)$ interpolate $f(x) \cdot \text{pdf}(x)$

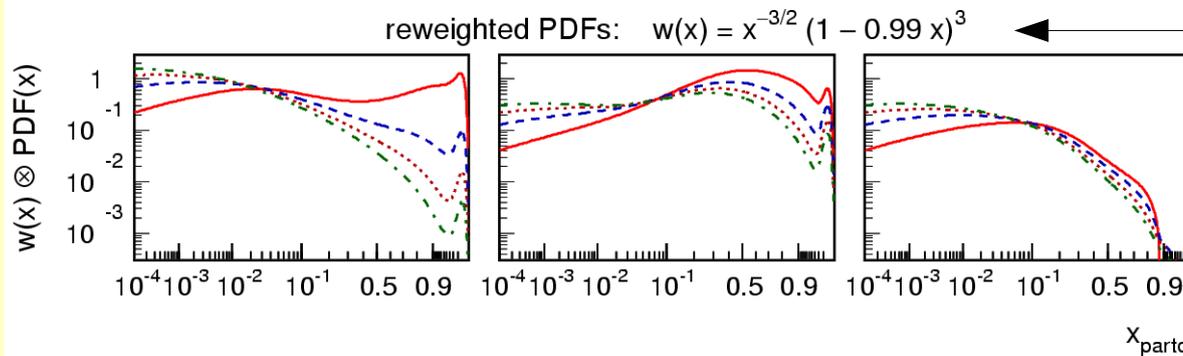
After reweighting: use cubic interpolation for remaining curvature...

before



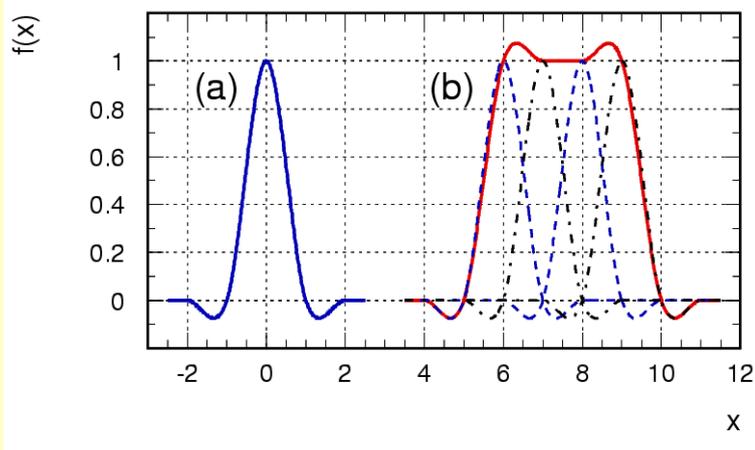
reweighting function

after

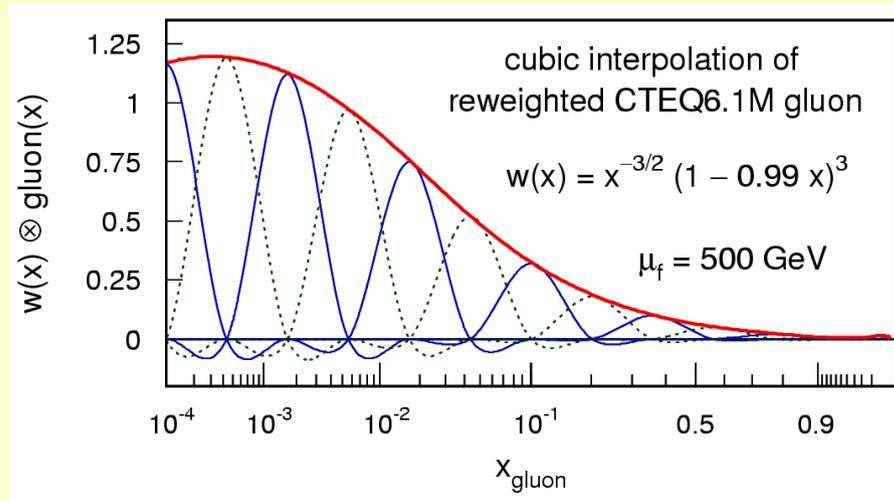
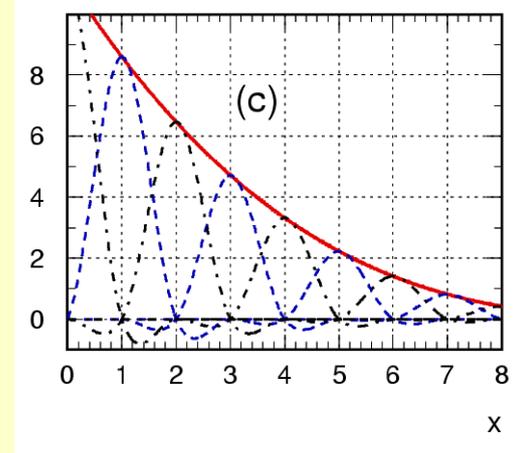


Cubic Interpolation

Several Eigenfunctions a).....



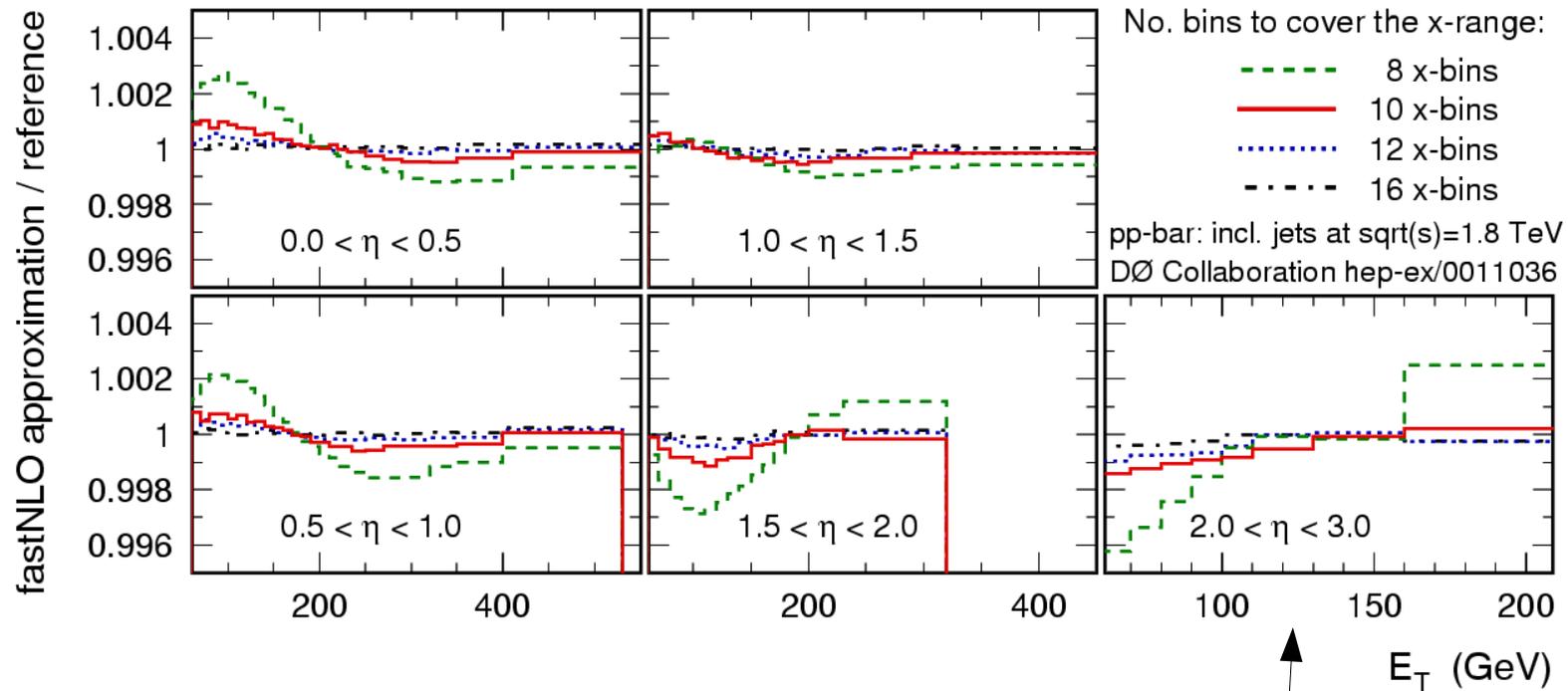
...approximate nicely a curved function c) ...



...such as a reweighted gluon density, with only 12 “x-bins”

Precision

TEVATRON Run II



only 10 x-bins sufficient for precision of 0.1%, even in forward region

Scales

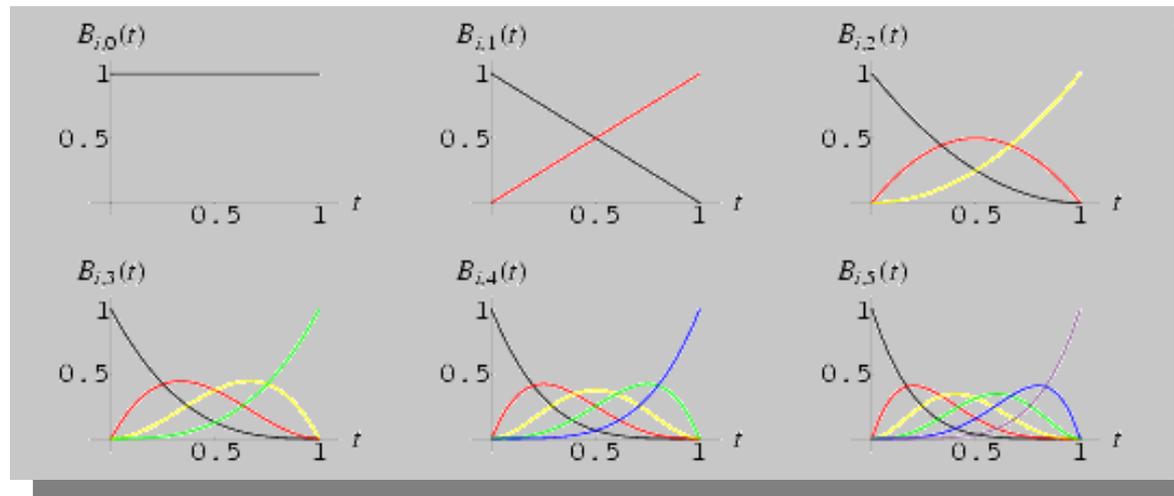
factorisation scale: choose between 4 scales: $1/4p_t$, $1/2p_t$, p_t , $2p_t$
renormalisation scale: arbitrary scale variation possible (for LO+NLO part)

Measured bins span range in jet p_t , what to choose when calculating table?

Bin center not exactly known (depends on pdf, α_s)...

Interpolate!

- 1) small p_t range: fixed scale at middle of bin
- 2) larger range: interpolation with Bernstein polynomials, (used e.g. for HERA jets)



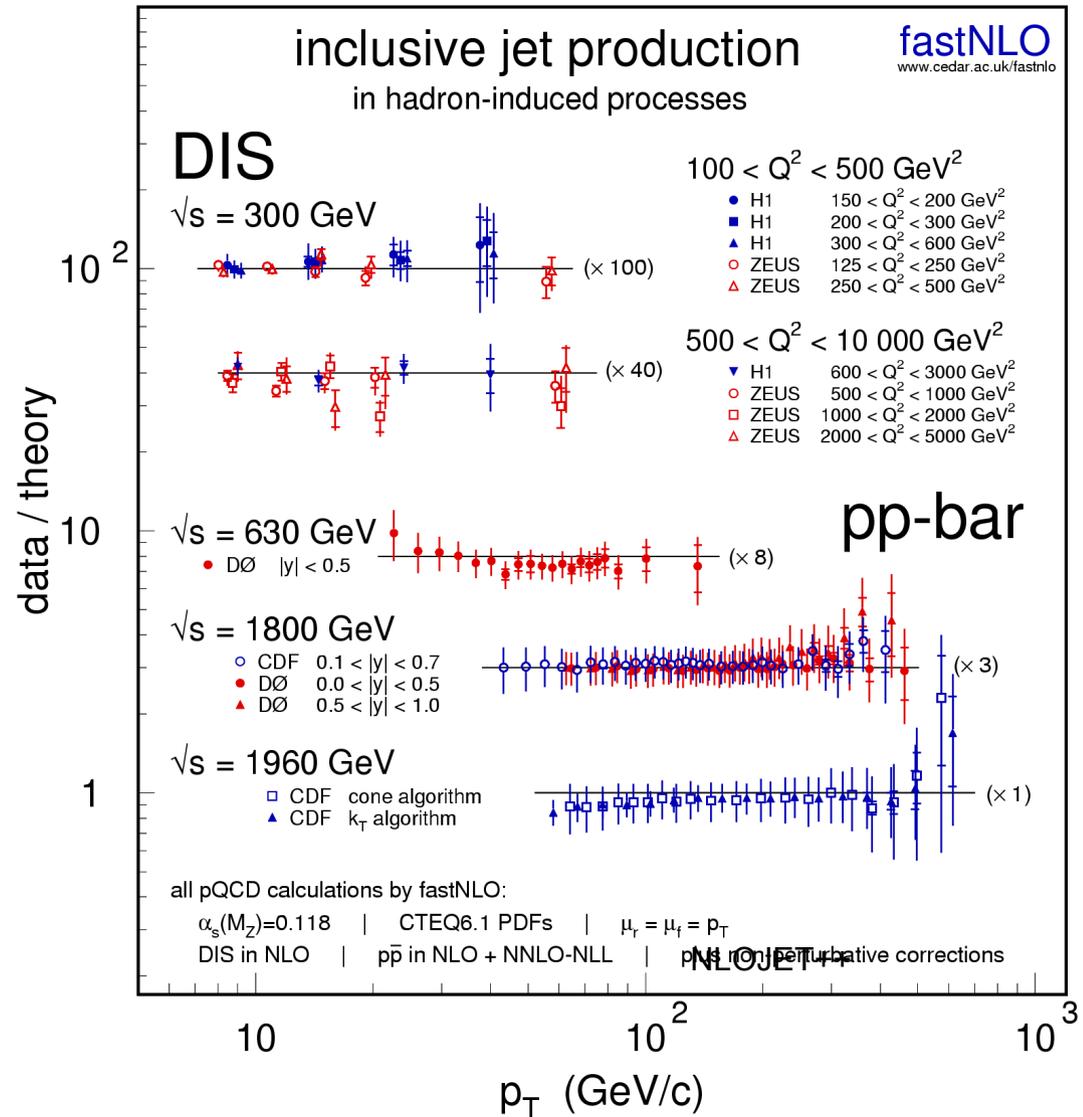
MathWorld

Inclusive jet data:
several processes, experiments,
center of mass energies and
 p_T ranges

Predictions obtained with fastNLO
based on NLOJET++, CTEQ 6.1 pdfs
and $\alpha_s(m_Z)=0.118$

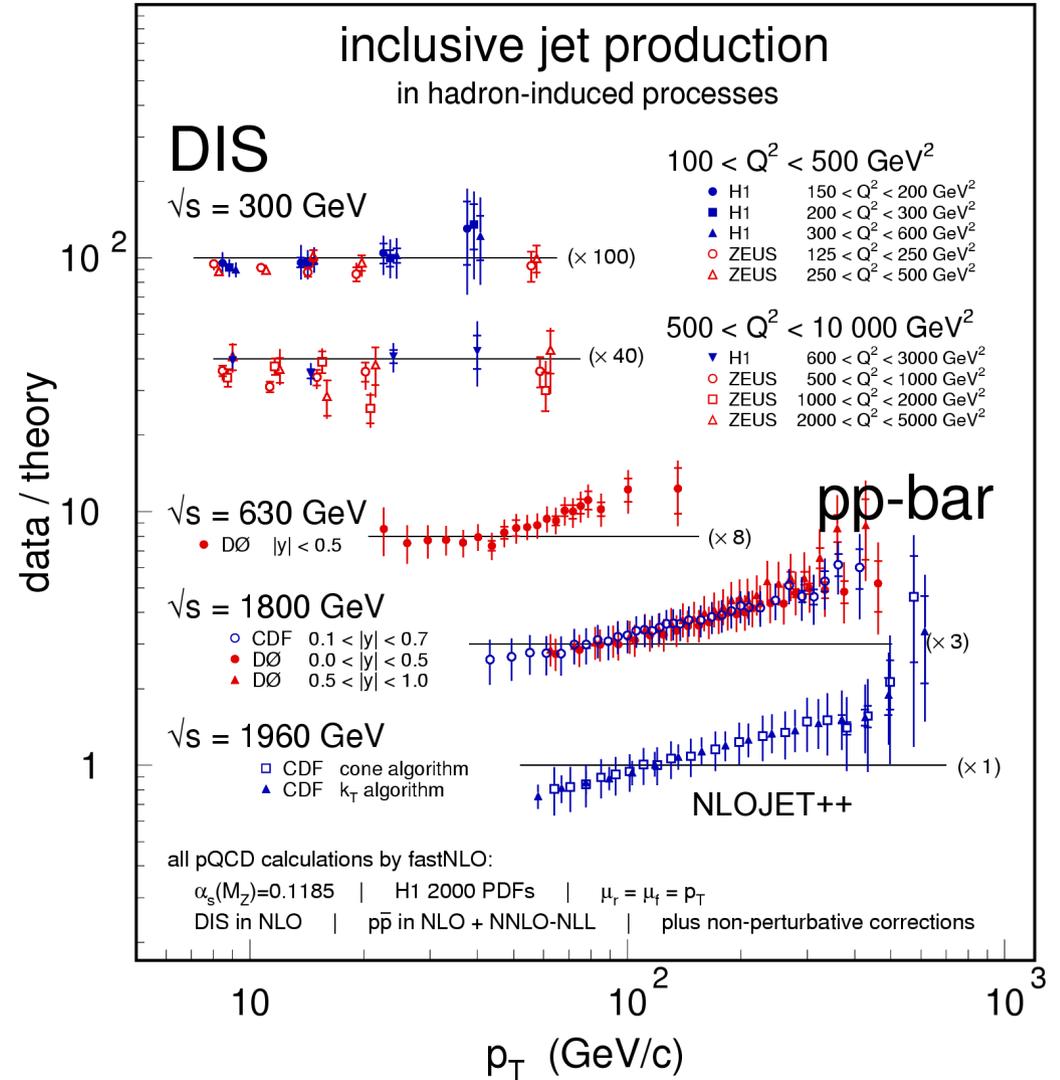
Good description of all the data

Can be used in fits!



The same, now with H1 2000 pdfs

This pdfs do not include jet data into fit
 Cannot describe TEVATRON jets,
 wrong p_t dependence
 Do not describe HERA jets neither,
 -> use jets in next fit!



Available Applications

LHC: pp @ sqrt(s)=14TeV

fnt2004 test-scenario for ATLAS, incl. jets, KT algo (pT, y)
code table

Tevatron Run II: pp-bar @ sqrt(s)=1.96TeV

fnt2001 DØ dijets, cone algo (DeltaPhi, pT)
hep-ex/0409040, (the data at Durham)
code table1 and table2

fnt2002 CDF incl. jets, cone algo (pT)
hep-ex/0512020, (the data at Durham)
code table (midpoint), table (Rsep)

fnt2003 CDF incl. jets, KT algo (pT)
hep-ex/0512062 (the data at Durham)
code table

HERA: ep @ sqrt(s)=300GeV or 320GeV

fnh1001 H1 incl. jets, KT algo (ET, Q2)
hep-ex/0010054 (see table 2 in hep-ex/0010054)
code table

fnh1002 ZEUS incl. jets, KT algo (ET, Q2)
hep-ex/0208037 (the data at Durham)
code table

fnh1003 H1 incl. jets, KT algo (ET) @low Q2
hep-ex/0206029 (the data at Durham)
code table

fnh1004 H1 dijets, KT algo (ET, Q2)
hep-ex/0010054 (the data at Durham)
code table

RHIC: pp @ sqrt(s)=200GeV

fnr0001 STAR preliminary incl. jets, cone algo (pT)
code table (midpoint)

Tevatron Run I: pp-bar @ sqrt(s)=1.8TeV

fnt1001 CDF incl. jets, cone algo (ET)
hep-ph/0102074 (the data at Durham)
code table (midpoint), table (Rsep)

fnt1002 DØ incl. jets, cone algo (ET, eta)
hep-ex/0011036 (the data at Durham)
code table (midpoint), table (Rsep)

fnt1003 CDF dijets, cone algo (ET, eta1, eta2)
hep-ex/0012013 (the data at Durham)
code table (midpoint), table (Rsep)

fnt1004 DØ incl. jets @ sqrt(s)=630GeV, cone algo (ET)
hep-ex/0012046 (the data at Durham)
code table (midpoint), table (Rsep)

fnt1005 DØ incl. jets, ratio 630/1800GeV, cone algo (xT)
hep-ex/0012046 (the data at Durham)
code table1, table2 (midpoint) or table1 table2 (Rsep)

fnt1007 CDF dijets, cone algo (mass)
hep-ex/9912022 (the data at Durham)
code table (midpoint), table (Rsep)

fnt1008 DØ dijets, cone algo (mass)
hep-ex/0012046 (the data at Durham)
code table (midpoint), table (Rsep)

**All with high statistics,
typically 6 CPU months**

**Combined effort of
H1 Farm, D0 Farm and GRID**

Web Interface to fastNLO

<http://hepforge.cedar.ac.uk/fastnlo>

fastNLO

hosted by CEDAR HepForge

fast pQCD calculations for hadron-induced processes

Home

Documentation

Interactive

Code

Links

Interactive Web Interface

Here you can compute the pQCD theory predictions in LO and NLO for all observables accessible in the pull down menu.

For the inclusive jet cross section in hadron collisions also the 2-loop threshold corrections are computed (restriction: the latter is available only for $\mu_r = \mu_f$).

select Observable:

fhl0004 - LHC - ATLAS incl jets (kT - pt, y) - test scenario

Proton PDFs: CTEQ6.1M - NLO

PDF members: best fit - for alpha-s(Mz)=0.118

alpha-s(Mz): 0.118 (used in the matrixelement)

factorization scale: $\mu_f = 1$ * pT or ET (whatever was used in the jet definition)

renormalization scale: $\mu_r = 0.0$ * pT or ET (set to zero to get: $\mu_r = \mu_f$)

(please note that for μ_r different from μ_f the threshold corrections for inclusive jets in pp are not available)

output: (so far only ASCII output is working)

- ASCII
- plot observable: data and theory
- plot ratio: data/theory

do the calculation

Thomas Kluge, Klaus Rabbertz, Markus Wobisch
(send mail to the authors: fastnlo@cedar.ac.uk)

fhl0004 - LHC - ATLAS incl jets (kT - pt, y) - test scenario
fnt2004 - Tevatron Run II - CDF incl jets (kT - pT, y) - preliminary
fnt2003 - Tevatron Run II - CDF incl jets (kT - pT) - hep-ex-0512062
fnt2002 - Tevatron Run II - CDF incl jets (cone - pT) - hep-ex-0512020
fnt1001 - Tevatron Run I - CDF incl jets (cone - ET) - hep-ph/0102074
fnt1002 - Tevatron Run I - D0 incl jets (cone - ET, eta) - hep-ex/0011036
fnt1003 - Tevatron Run I - CDF dijets (cone - ET, eta1, eta2) - hep-ex/0012013
fnt1004 - Tevatron Run I @630GeV - D0 incl jets (cone - ET) - hep-ex/0012046
fnt1007 - Tevatron Run I - CDF dijets (cone - mass) - hep-ex/9912022
fnt1008 - Tevatron Run I - D0 dijets (cone - mass) - hep-ex/0012046
fnh1001 - HERA - DIS incl jets - H1 (kT - ET, Q2) - hep-ex/0010054
fnh1002 - HERA - DIS incl jets - ZEUS (kT - ET, Q2) - hep-ex/0208037
fnh1003 - HERA - DIS fwd jets - H1 (kT - ET, ET) - hep-ex/0206029
fnh1004 - HERA - DIS dijets - H1 (kT - ET, Q2) - hep-ex/0010054
fnr0001 - RHIC - STAR incl jets (cone - pT, eta) in pp at sqrt(s)=200GeV

0.25
0.5
1
2

best fit A118 - for alpha-s(Mz)=0.118

A110 - alpha-s(Mz)=0.110
A112 - alpha-s(Mz)=0.112
A114 - alpha-s(Mz)=0.114
A116 - alpha-s(Mz)=0.116
A120 - alpha-s(Mz)=0.120
A122 - alpha-s(Mz)=0.122
A124 - alpha-s(Mz)=0.124
A126 - alpha-s(Mz)=0.126
A128 - alpha-s(Mz)=0.128
B110 - alpha-s(Mz)=0.110
B112 - alpha-s(Mz)=0.112
B114 - alpha-s(Mz)=0.114
B116 - alpha-s(Mz)=0.116
B118 - alpha-s(Mz)=0.118
B120 - alpha-s(Mz)=0.120
B122 - alpha-s(Mz)=0.122
B124 - alpha-s(Mz)=0.124
B126 - alpha-s(Mz)=0.126
B128 - alpha-s(Mz)=0.128

CTEQ6.1M - NLO
CTEQ6AB - NLO
CTEQ5M1 - NLO
CTEQ4M - NLO
MRST2004 - NNLO
MRST2004 - NLO
MRST2002 - NNLO
MRST2002 - NLO
MRST2003c - NNLO
MRST2003c - NLO
Alekhin 2002 - NNLO
Alekhin 2002 - NLO
ZEUS 2005 Jet Fit (ZJ) - NLO
H1 2000 MS-bar - NLO
FERMI 2002 - NLO
Botje99 - NLO

Choose measurement, pdf set and member, α_s and scales....

Web Interface to fastNLO

```

fastNLO: compute the cross section
# #####
#
# fastNLO - version 1.4      Jan. 31, 2006
#
# Thomas Kluge, Klaus Rabbertz, Markus Wobisch
#
# if you use this code, please cite as reference:
#   T. Kluge, K. Rabbertz and M. Wobisch,
#   publication in preparation,
#   (hep-ex No. to be added)
#
# ... now reading the coefficient table:
# tableformat is version 1.4
# 26200000000 events in LO
# 24600000000 events in NLO
# 2764800 events in NNLO-NLL-(threshold-corrections)
# No. of x bins: 12
#
# this table contains: d2sigma-jet_dpT_dy_(pb_GeV)
# as published in:    not-published
# by:                 ATLAS-test-scenario
#
# reaction: proton-proton
# process: inclusive jets
# total No. of observable bins: 103
# jet algo: kt algorithm
#   parameter 1: D = 0.7
#   parameter 2: n/a = 0.
#
# the single contributions have been computed
# using the following codes:
# LO
#   by: NLOJET++
# NLO
#   by: NLOJET++
# NNLO-NLL-(threshold-corrections)
#   by: Kidonakis-Owens
#
# for NLOJET++ please cite:
#   Z. Nagy, Phys. Rev. Lett. 88, 122003 (2002),
#   Z. Nagy, Phys. Rev. D68, 094002 (2003).
#
# the 2-loop threshold corrections for the inclusive jet
# cross section in pp and pbar have been computed by:
# N. Kidonakis and J.F. Owens - please cite
# N. Kidonakis, J.F. Owens, Phys. Rev. D63, 054019 (2001).

```

```

-- fastNLO - results for d2sigma-jet_dpT_dy_(pb_GeV)
-- cross sections:      LO      NLOcorr      2-loop      total
----- mu_f/mu_0= 1.      mu_r/mu_0= 1.
      from 0. - 0.8 in: y
pT_in_GeV  60.00- 80.00:  0.1300E+06  0.2101E+05  0.2955E+05  0.1805E+06
pT_in_GeV  80.00- 100.00: 0.3811E+05  0.6493E+04  0.7745E+04  0.5235E+05
pT_in_GeV 100.00- 130.00: 0.1184E+05  0.1977E+04  0.2197E+04  0.1602E+05
pT_in_GeV 130.00- 160.00: 0.3617E+04  0.6351E+03  0.6145E+03  0.4866E+04
pT_in_GeV 160.00- 200.00: 0.1210E+04  0.2100E+03  0.1911E+03  0.1611E+04
pT_in_GeV 200.00- 250.00: 0.3766E+03  0.6726E+02  0.5525E+02  0.4991E+03
pT_in_GeV 250.00- 300.00: 0.1256E+03  0.2277E+02  0.1723E+02  0.1656E+03
pT_in_GeV 300.00- 350.00: 0.4964E+02  0.9113E+01  0.6447E+01  0.6520E+02
pT_in_GeV 350.00- 400.00: 0.2211E+02  0.4131E+01  0.2742E+01  0.2898E+02
pT_in_GeV 400.00- 450.00: 0.1079E+02  0.2067E+01  0.1285E+01  0.1414E+02
pT_in_GeV 450.00- 500.00: 0.5650E+01  0.1087E+01  0.6497E+00  0.7387E+01
pT_in_GeV 500.00- 600.00: 0.2476E+01  0.4901E+00  0.2730E+00  0.3239E+01
pT_in_GeV 600.00- 700.00: 0.8916E+00  0.1813E+00  0.9326E-01  0.1166E+01
pT_in_GeV 700.00- 800.00: 0.3642E+00  0.7596E-01  0.3645E-01  0.4766E+00
pT_in_GeV 800.00- 900.00: 0.1635E+00  0.3504E-01  0.1576E-01  0.2143E+00
pT_in_GeV 900.00- 1000.00: 0.7893E-01  0.1733E-01  0.7368E-02  0.1036E+00
pT_in_GeV 1000.00- 1200.00: 0.3095E-01  0.7007E-02  0.2788E-02  0.4074E-01
pT_in_GeV 1200.00- 1400.00: 0.9430E-02  0.2238E-02  0.8150E-03  0.1248E-01
pT_in_GeV 1400.00- 1600.00: 0.3234E-02  0.8099E-03  0.2718E-03  0.4316E-02
pT_in_GeV 1600.00- 1800.00: 0.1205E-02  0.3129E-03  0.9957E-04  0.1618E-02
pT_in_GeV 1800.00- 2000.00: 0.4759E-03  0.1284E-03  0.3905E-04  0.6434E-03
pT_in_GeV 2000.00- 2200.00: 0.1958E-03  0.5551E-04  0.1611E-04  0.2674E-03
pT_in_GeV 2200.00- 2400.00: 0.8285E-04  0.2437E-04  0.6895E-05  0.1141E-03
pT_in_GeV 2400.00- 2600.00: 0.3568E-04  0.1095E-04  0.3028E-05  0.4966E-04
pT_in_GeV 2600.00- 2800.00: 0.1552E-04  0.4956E-05  0.1353E-05  0.2183E-04
pT_in_GeV 2800.00- 3000.00: 0.6765E-05  0.2256E-05  0.6106E-06  0.9631E-05
pT_in_GeV 3000.00- 3500.00: 0.1811E-05  0.6408E-06  0.1739E-06  0.2626E-05
pT_in_GeV 3500.00- 4500.00: 0.1154E-06  0.4618E-07  0.1292E-07  0.1745E-06
      from 0.8 - 1.6 in: y
pT_in_GeV  60.00- 80.00:  0.1160E+06  0.1968E+05  0.2947E+05  0.1651E+06
pT_in_GeV  80.00- 100.00: 0.3347E+05  0.5487E+04  0.7472E+04  0.4643E+05
pT_in_GeV 100.00- 130.00: 0.1025E+05  0.1792E+04  0.2056E+04  0.1410E+05
pT_in_GeV 130.00- 160.00: 0.3078E+04  0.5313E+03  0.5566E+03  0.4166E+04
pT_in_GeV 160.00- 200.00: 0.1014E+04  0.1786E+03  0.1682E+03  0.1361E+04
pT_in_GeV 200.00- 250.00: 0.3106E+03  0.5500E+02  0.4717E+02  0.4128E+03
pT_in_GeV 250.00- 300.00: 0.1019E+03  0.1854E+02  0.1425E+02  0.1347E+03
pT_in_GeV 300.00- 350.00: 0.3963E+02  0.7346E+01  0.5181E+01  0.5216E+02

```

... and obtain a second later cross sections, precision based on months of CPU time

Summary

- Available: fastNLO on the web with jet observables from
 - HERA, TEVATRON, RHIC, LHC
 - LO+NLO (NLOJET++), hadron-hadron: 2-loop threshold corrections
- After >1 year of hard work (beta released 9 months ago):
Ready, download **now**: code to be used for fits, instructions how to use
 - needs 0.5ms per point
 - precision typically better than 0.1%
 - ... to be used in global pdf fits
- Plans:
 - include photoproduction (when included in NLOJET++)
 - other processes, Drell-Yan, ...
- Towards V2.0:
 - establish future proof standard for tables, XML (code exists, using Xerces DOM)
 - fastNLO could be a common repository of calculations (not only NLO), together with www.arXiv.org and Durham database -> future impact of today measurements